

Lecture 19: Mandelbrot and Sequential Consistency

COSC 273: Parallel and Distributed
Computing

Spring 2023

Announcements

1. Lab 03 Due ~~Friday~~ MONDAY!!

- Mandelbrot computations using Vector operations
- Make sure your machine supports Vector ops **today**:

```
> javac --add-modules jdk.incubator.vector SomeFile.java  
> java --add-modules jdk.incubator.vector SomeFile
```

on HPC cluster, first run

```
> module load amh-java/19.0.1
```

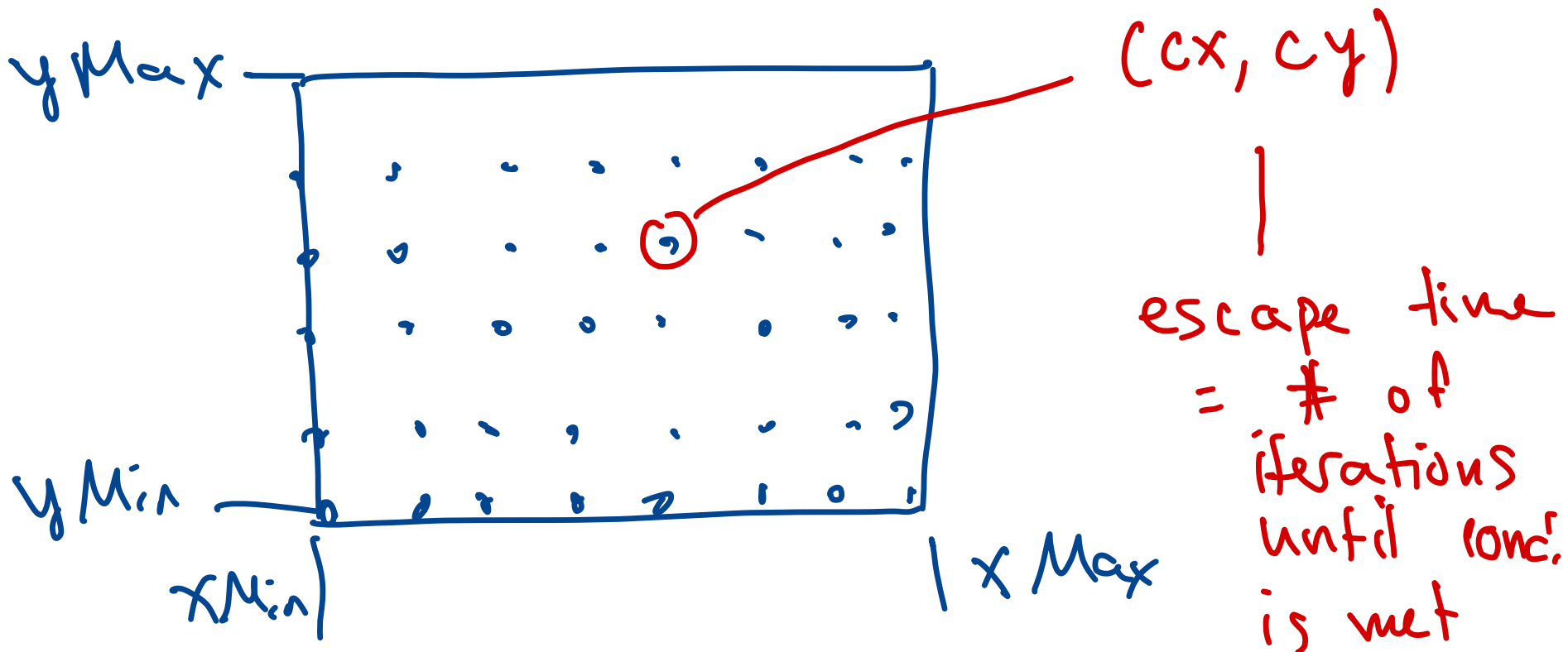
Today

1. Mandelbrot and Vectors
2. A Sequentially Consistent Queue

Mandelbrot with Vectors

Mandelbrot, High Level

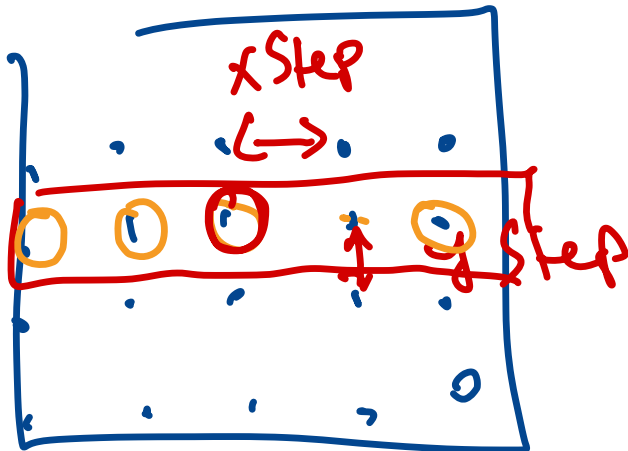
1. Define a grid of points
2. For each point
 - repeat until some condition is met:
 - perform arithmetic
 - record number of iterations



Baseline Code

```
float xStep = (xMax - xMin) / esc[0].length;
float yStep = (yMax - yMin) / esc.length;
for (int i = 0; i < esc.length; i++) {
  for (int j = 0; j < esc[0].length; j++) {
    int iter = 0;
    float cx = xMin + j * xStep;
    float cy = yMin + i * yStep;
    // do some arithmetic //
    esc[i][j] = iter;
  }
}
```

$i =$
row



$i =$ a row
 $j =$ a col

Baseline Code: Arithmetic

```
float zx = 0; float zy = 0;
while (iter < maxIter && zx * zx + zy * zy < maxSquareModulus) {
    float z = zx * zx - zy * zy + cx;
    zy = 2 * zx * zy + cy;
    zx = z;
    iter++;
}
esc[i][j] = iter; ←
```

When to
confine

Observation

This code is the same for all points!

```
float zx = 0; float zy = 0;
while (iter < maxIter && zx * zx + zy * zy < maxSquareModulus) {
    float z = zx * zx - zy * zy + cx;
    zy = 2 * zx * zy + cy;
    zx = z;
    iter++;
}
```

Differences:

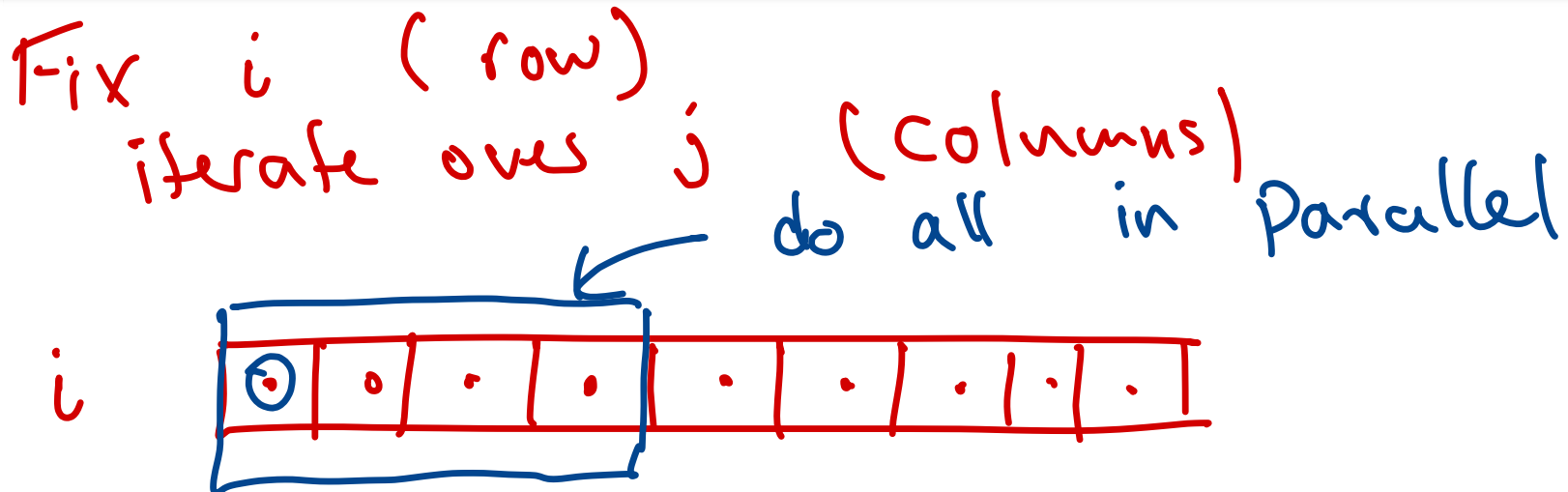
1. input data (cx and cy)
2. stopping time (when while condition is not satisfied)

What Can Be Vectorized?

```
for (int i = 0; i < esc.length; i++) {  
  for (int j = 0; j < esc[0].length; j++) {  
    int iter = 0;   
    float cx = xMin + j * xStep;   
    float cy = yMin + i * yStep;   
    float zx = 0; float zy = 0;   
    while(/* some condition */) { /* do stuff */  
      esc[i][j] = iter;   
    }  
  }  
}
```

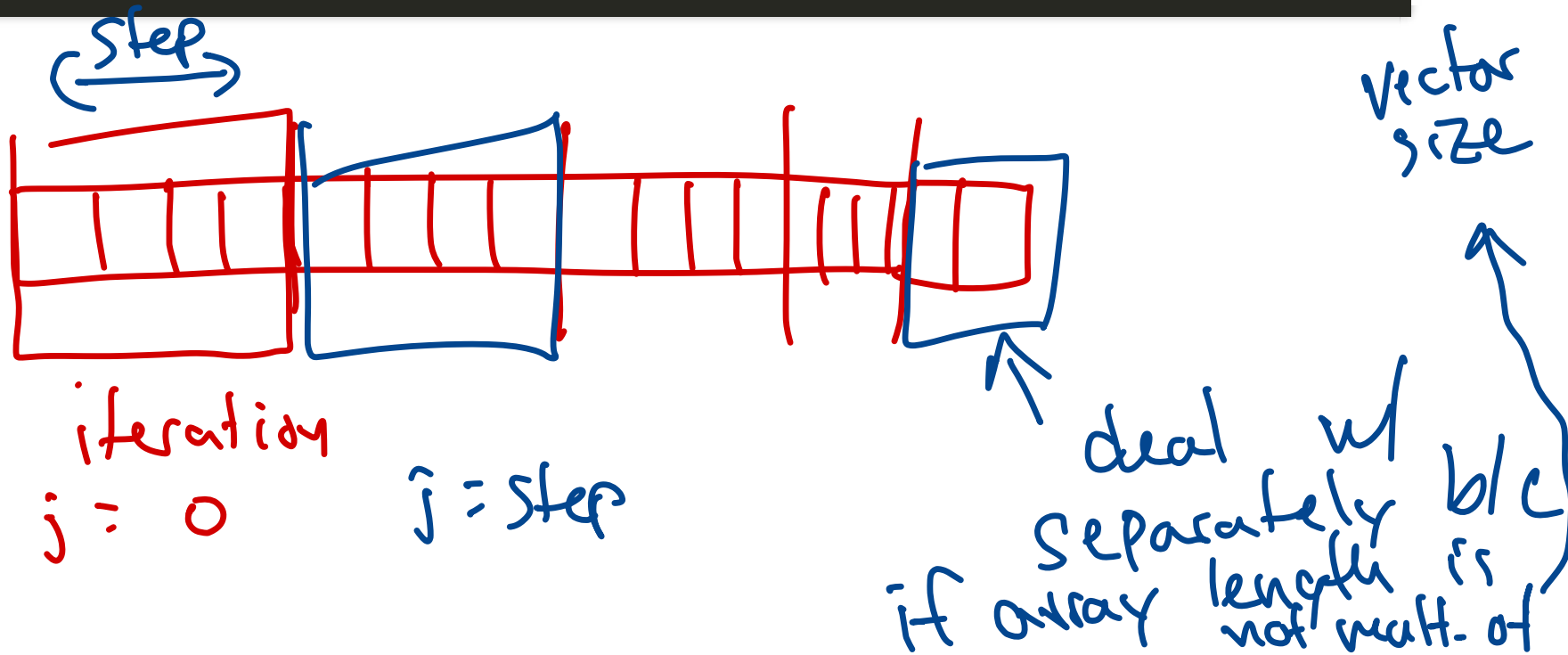
vectors

vector assignment to array



New Inner Loop Structure

```
int step = /*something*/;  
int max = /*something*/;  
int j = 0;  
for (j < max; j += step) {  
  
    /* initialize iter, cx, cy, zx, zy */  
  
    /* do arithmetic */  
  
}
```



How to Initialize Vectors?

- iter ← all lanes take val 0
 - previously 0
- cy ← compare to "broadcast" method
 - previously $yMin + i * yStep$

$cy \leftarrow \text{FloatVector.broadcast}(S \rightarrow, val)$

- cx
 - previously $cx = xMin + [j] * xStep$

1.0	1.1	1.2	1.3
-----	-----	-----	-----

$xStep = 0.1$

- zx, zy

↑
vectors of
0s

Start w/
+

1.0	1.0	1.0	1.0
0	0	0	0

0.0	0.1	0.2	0.2
-----	-----	-----	-----

How to Perform Vector Arithmetic?

```
while (iter < maxIter && zx * zx + zy * zy < maxSquareModulus) {  
vector float z = zx * zx - zy * zy + cx;      mul, sub, add  
  zy = 2 * zx * zy + cy;  
  zx = z;  
  iter++;  
}  
esc[i][j] = iter; true if condition still true for that lane
```

for each lane stop incrementing iter on that lane when condition is met for that lane

MASK

How To Check Termination?

```
while (iter < maxIter && zx * zx + zy * zy < maxSquareModulus) {  
    float z = zx * zx - zy * zy + cx;  
    zy = 2 * zx * zy + cy;  
    zx = z;  
    iter++;  
}  
esc[i][j] = iter;
```

No lanes are still true for
bit mask

→ look @ documentation
for Vector Mask

General Advice

1. Start with “direct” translation of baseline code
 - **READ THE *Vector* DOCUMENTATION**
 - use masked operations/conditions on masks
2. Test variations
 - tradeoff: variables vs operations

Sequential Consistency

Concurrent Objects

1. An ADT (abstract data type) defines *sequential* correctness of an object
 - e.g., queue, stack, set, etc.
2. Concurrent objects allow for concurrent operations on the object

Rhetorical Question. What does it mean for a concurrent object to be “correct?”

Sequential Consistency

An execution is **sequentially consistent** if all method calls can be ordered such that:

1. they are consistent with program order
2. they meet object's sequential specification

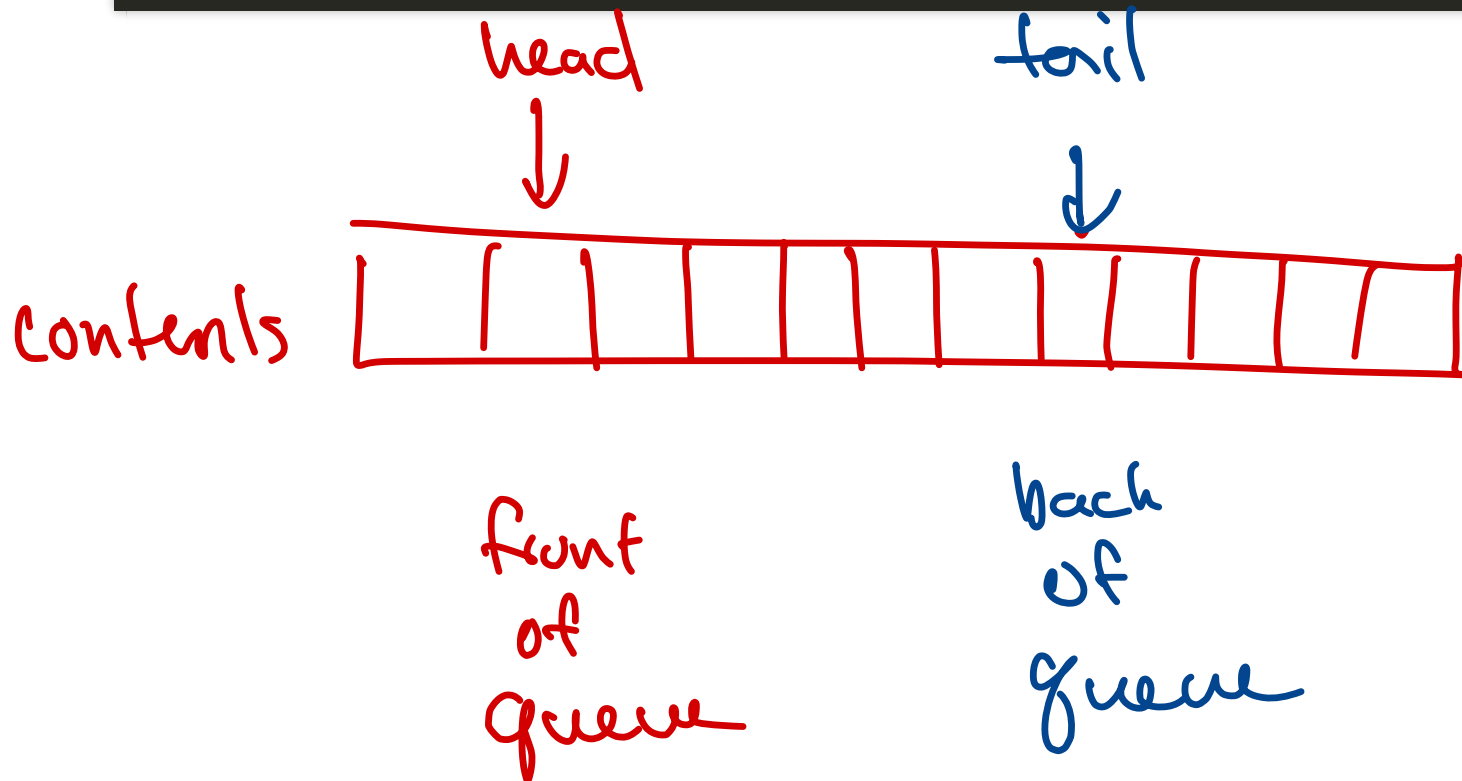
An implementation of an object is sequentially consistent if

1. it guarantees *every* execution is sequentially consistent

Example: A Sequentially Consistent Queue

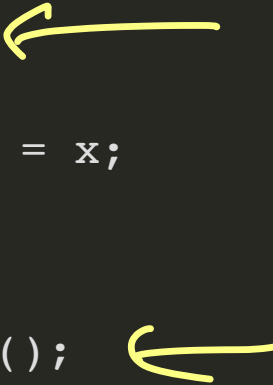
An Array-Based Queue

```
public class LockedQueue<T> {  
    int head, tail;  
    T[] contents;  
    Lock lock;   
}
```



Enqueuing

```
public void enq(T x) {  
    lock.lock();  
    try {  
        items[tail] = x;  
        tail++;  
    } finally {  
        lock.unlock();  
    }  
}
```

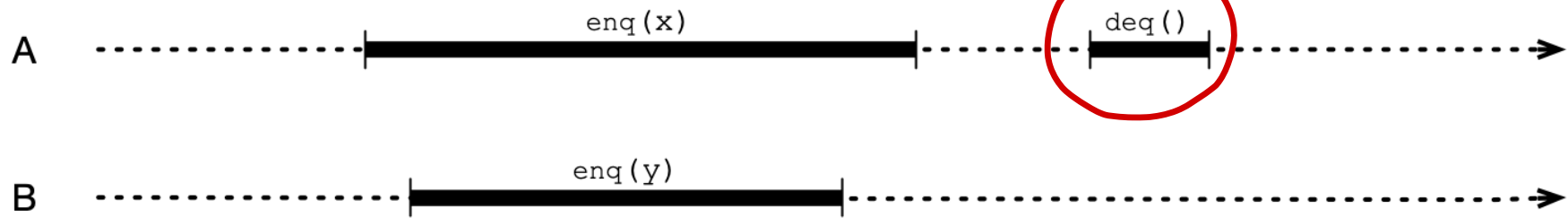


Dequeuing

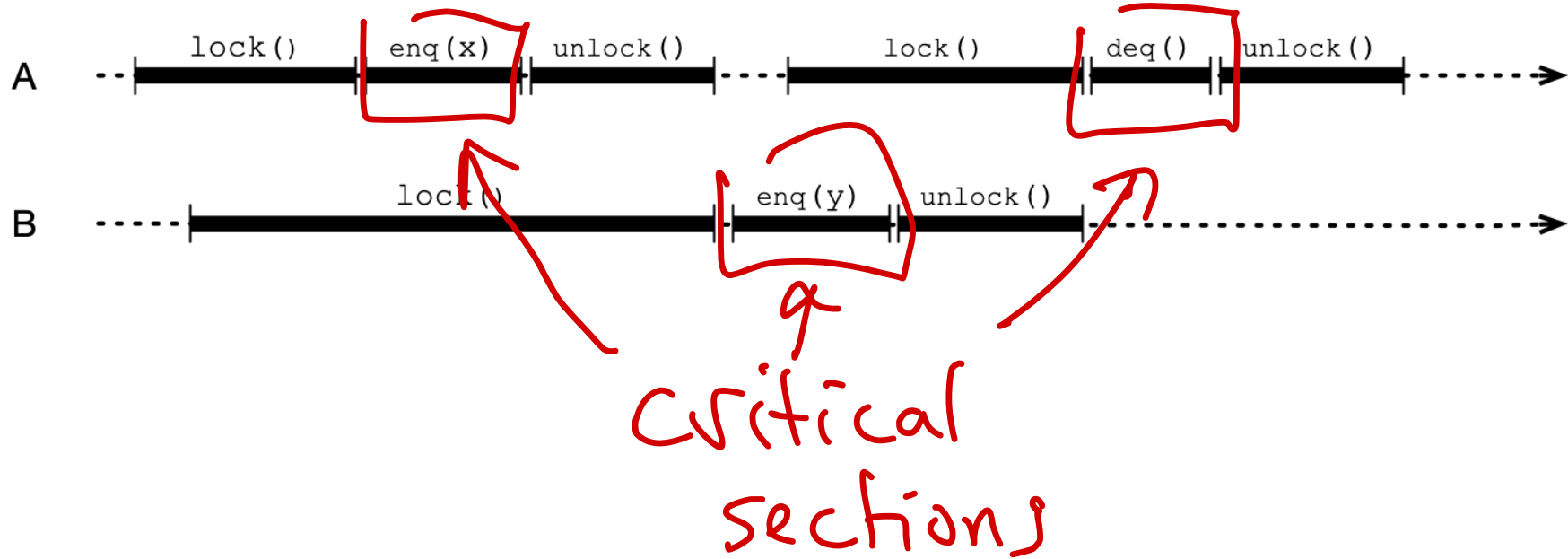
```
public T deq() {  
    lock.lock();  
    try {  
        T x = items[head];  
        head++;  
        return x;  
    } finally {  
        lock.unlock();  
    }  
}
```

What Happens?

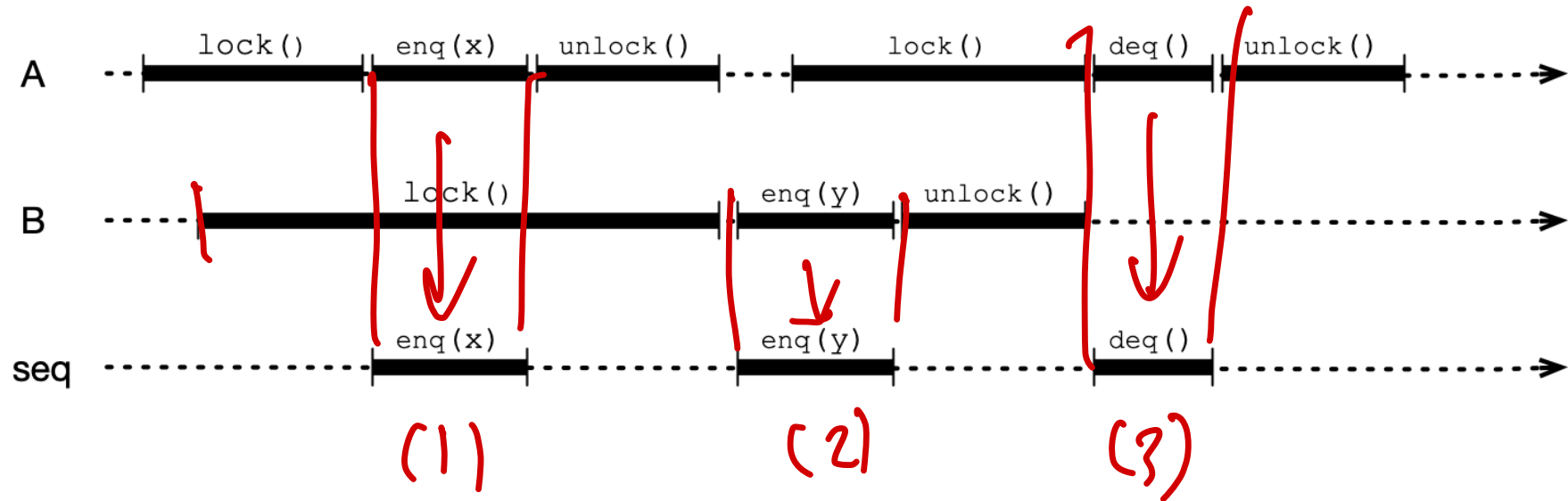
could return
x or y



What Happens with Locks?



Equivalent Sequential Execution

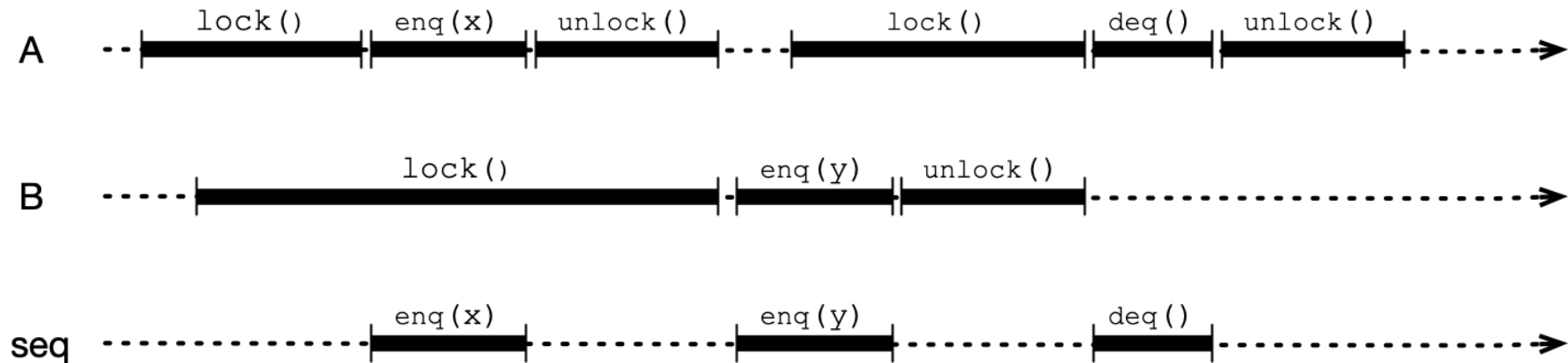


Why is Queue Sequentially Consistent?

Why is Queue Sequentially Consistent?

Locks!

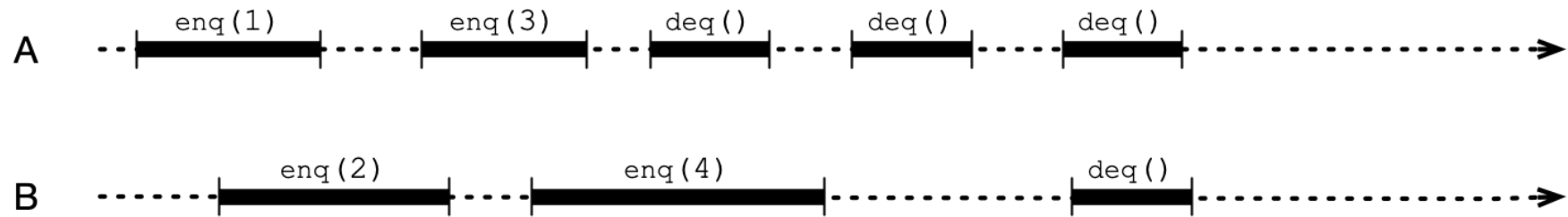
- mutual exclusion property of the Lock ensures that enq/deq operations are **not concurrent**
- calls to enq/deq can be ordered according to “wall clock” time of execution of critical sections



Questions

1. Can we achieve sequential consistency without resorting to locks?
 - again, this technique is essentially sequential
2. Is sequential consistency enough?

What are “Acceptable” Outcomes?



Next Time

Linearizability: A *stronger* notion of correctness for concurrent objects

- considers “wall clock” time in addition of program order

